

Variance in Steady-State Simulation Optimization: Key Challenges and Algorithms

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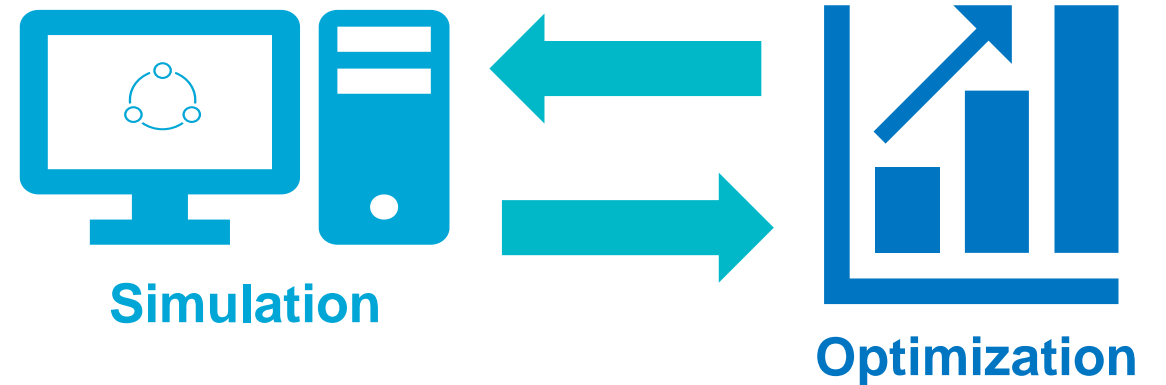
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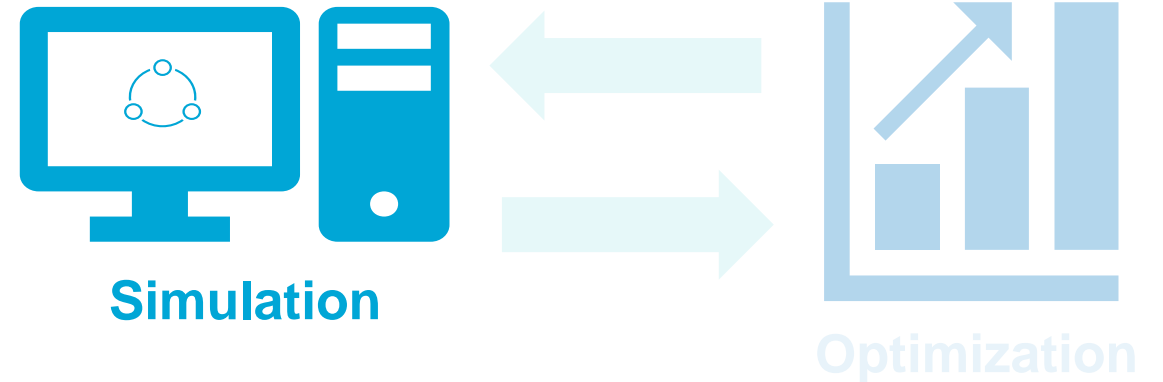
Simulation Optimization

- Model complex (stochastic) systems
- Optimize these models
- Support decision making
- Explore large solution spaces



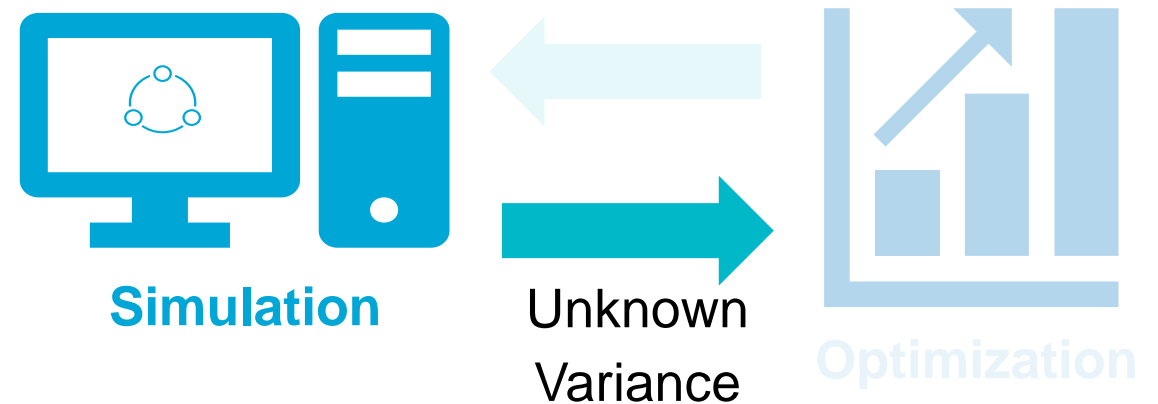
Simulation

- Simulate until steady state
- Simulation variability (finite run time)
- Parameter variability (input data)



Problem statement

- Variability in Simulation **output**,
thus variability in optimizer **input**
- Variance is unknown (late '60)
- Conway: batches



Optimization



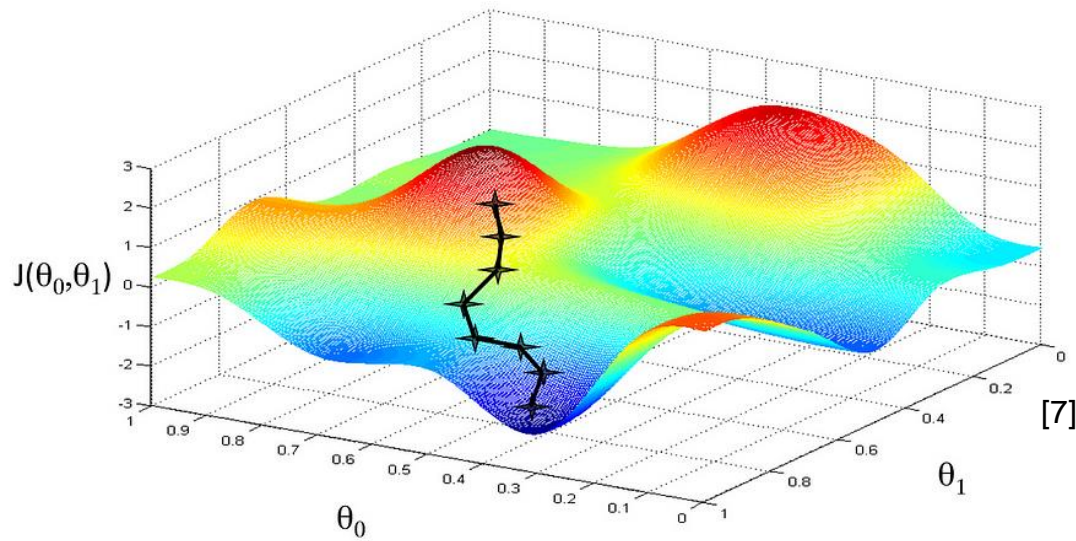
Simulation



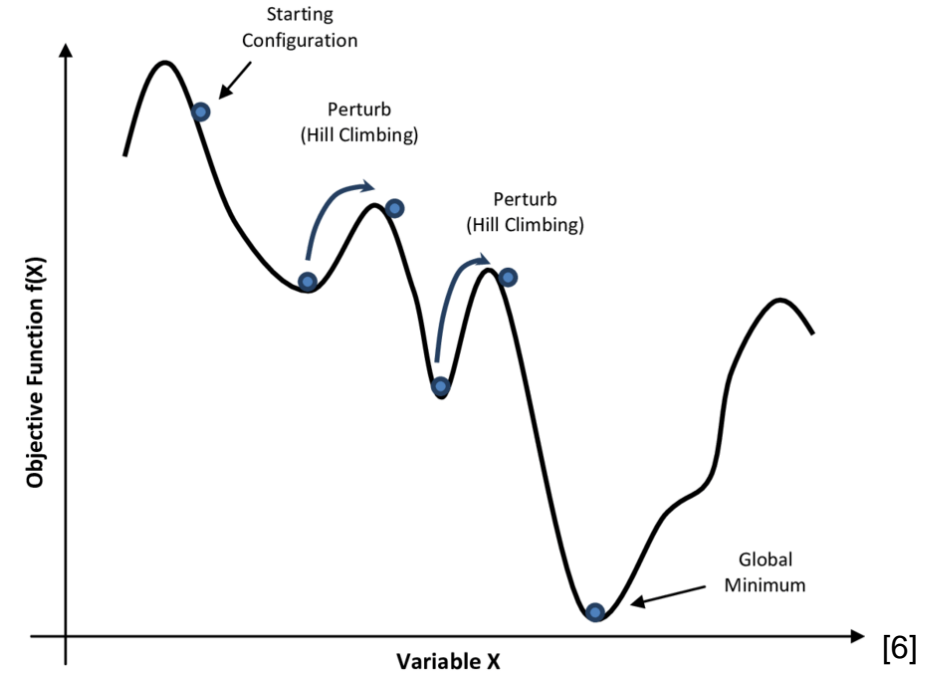
Optimization

Stochasticity in Optimization Models

Two classes of classification methods:



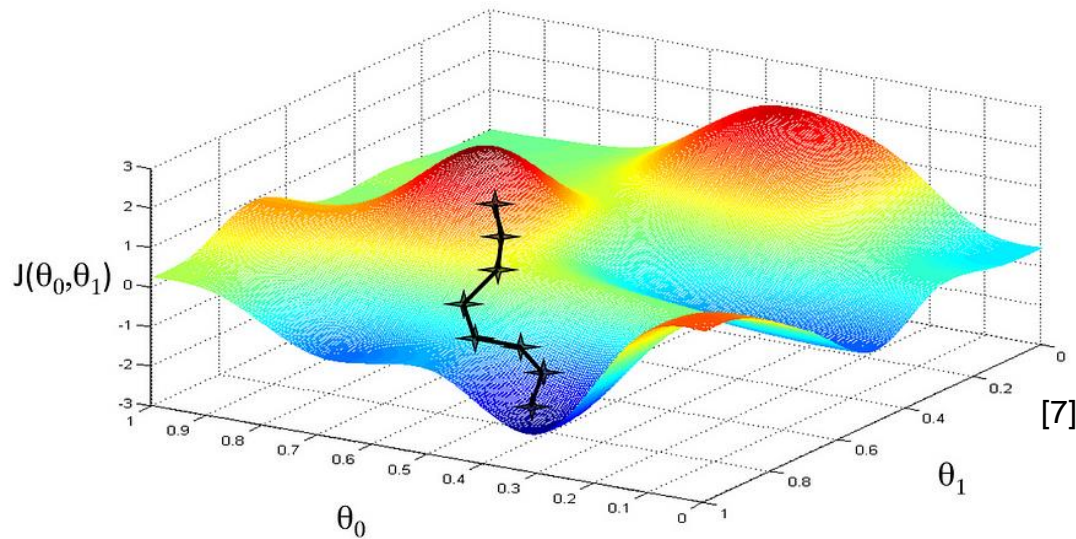
Mathematical Optimization



Approximate Algorithms



Stochasticity in Optimization Models



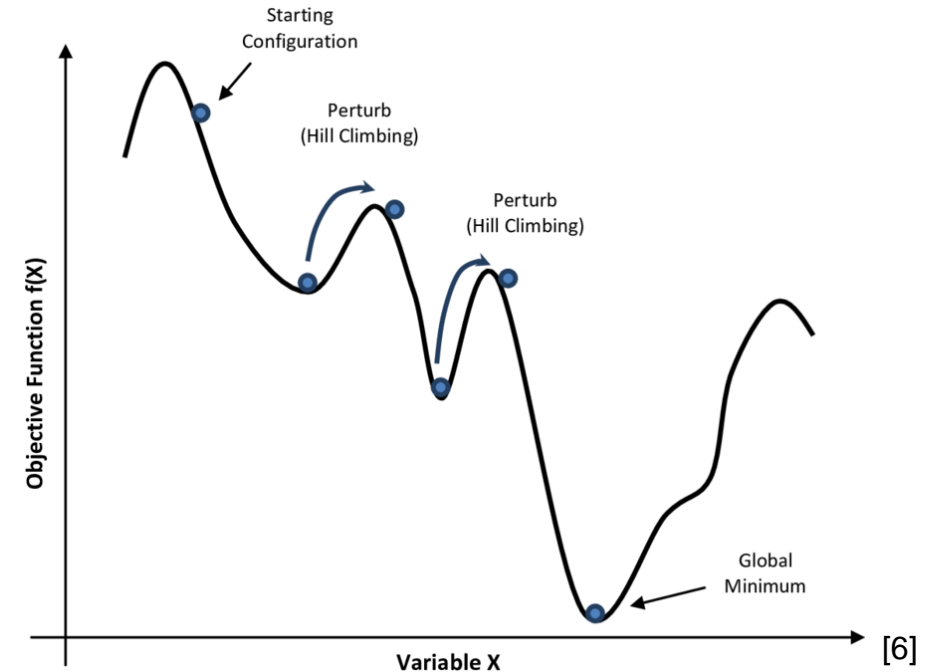
Mathematical Optimization



- Combination of techniques and methods for finding optimum within a set of constraints^[1]
- Examples are **linear optimization** and **non-linear optimization**^[1]
- **Use cases** for simulation-based optimization:
 - Sensitivity analysis^[2]
 - Validation of starting points & solutions^[3]
- **Problems** through stochasticity:
 - Need of precise values

Stochasticity in Optimization Models

- Focus on quick good solutions rather than finding optimal solutions
- Examples are **heuristics** and **metaheuristics** [4]
- **Use cases** for simulation-based optimization:
 - Comparison of different strategies [5]
 - Validation of solutions [5]
- **Problems** through stochasticity:
 - Interpretation of simulation results becomes more difficult



Approximate Algorithms



Variance in Simulation output



Simulation



Unknown variance



Optimization



Asymptotic Normality Theory

Predictable distribution of simulation averages

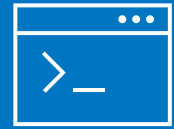
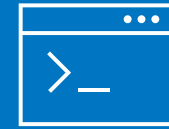
Based on Central Limit Theorem
Assumes finite variance
Assumes not fat tailed distribution
Assumes large sample size
Results in confidence intervals
Uses Gaussian distribution



Bootstrapping

Resampling to estimate variability without strong assumptions

Based on observed data
No assumptions
Less simulation runs needed
More computation needed

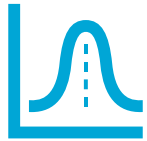


Direct Two-Point Method

Simple variance estimation through independent runs

Based on difference of two points
Assumes rough spread around the mean
Quick and simple
Not robust

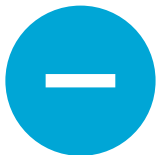
Possible combination with optimization models



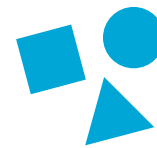
**Mathematical optimization
&
Asymptotic Normality
Theory**



Asymptotic Normality Theory enables precise values



High computational time for both simulation & optimization



**Approximate algorithms
&
Bootstrapping**



Better understanding of distribution

Metrics like VaR & CVaR can ensure robust performance ^[8]

Thank you for your attention!

References

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